

# Math 375 Midterm Topics Guide

1. Chapter 1: Complex Numbers
  - (a) the 4 definitions/viewpoints
  - (b) Algebraic properties
  - (c) conjugation
  - (d) topology
  - (e) calc theorems
2. Chapter 2: Differentiation
  - (a) limits
  - (b) derivative & holomorphic
  - (c) Cauchy-Riemann equations
  - (d) 0 derivative implies constant
3. Chapter 3: Examples of Functions
  - (a) Möbius transformations
  - (b) cross ratio
  - (c) infinity, stereographic projection, Riemann sphere
  - (d)  $\exp$ , trig functions
  - (e)  $\log$ ,  $\mathcal{L}og$ ,  $\mathcal{L}og$
4. Chapter 4: Integration
  - (a) Integral over a curve
  - (b) Homotopy
  - (c) Cauchy's Theorem
  - (d) Cauchy's Integral Formula
  - (e) Jordan Curve Theorem
5. Chapter 5: Consequences of Cauchy's Theorem
  - (a) Extensions of Cauchy's formula for derivatives
  - (b) Computing integrals using Cauchy formulas.