

## Quiz 2

September 17, 2010

0. I allow to return this and future graded quizzes (not exams) to me in a common pile so that other students can possibly see my grade (circle appropriate box)

Yes	No	Signature
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1. Let  $A$  be a matrix. Complete the following definitions

- (a) A column in matrix  $A$  is called pivot if *it contains a leading entry when  $A$  is reduced to REF.*
- (b) The rank of matrix  $A$  is *the number of pivot columns in  $A$*

2. Let

$$A = \begin{pmatrix} 0 & 1 & 2 \\ -1 & -2 & 1 \end{pmatrix}, \quad B = \begin{pmatrix} 2 & 0 & 1 \\ -1 & 0 & 1 \\ 3 & 0 & 0 \end{pmatrix}$$

State which of the following is defined and compute corresponding expressions.

- (a)  $AB$

$$AB = \begin{bmatrix} 0 & 1 & 2 \\ -1 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 & 0 & 1 \\ -1 & 0 & 1 \\ 3 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 0 \cdot 2 + 1 \cdot (-1) + 2 \cdot 3 & 0 \cdot 0 + 1 \cdot 0 + 2 \cdot 0 & 0 \cdot 1 + 1 \cdot 1 + 2 \cdot 0 \\ (-1) \cdot 2 + (-2) \cdot (-1) + 1 \cdot 3 & (-1) \cdot 0 + (-2) \cdot 0 + 1 \cdot 0 & (-1) \cdot 1 + (-2) \cdot 1 + 1 \cdot 0 \end{bmatrix} = \begin{bmatrix} 5 & 0 & 1 \\ 3 & 0 & -3 \end{bmatrix}$$

- (b)  $BA$

NOT DEFINED

- (c)  $A+B$

NOT DEFINED

- (d)  $2A$

$$2A = \begin{bmatrix} 0 & 2 & 4 \\ -2 & -4 & 2 \end{bmatrix}$$